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1	Linear Programming on Portfolio Optimization: Empirical
2	Evidence from Bist Mining Industry Index
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7 Abstract

8 A lot of methods are improved for the portfolio optimization within classical approach.

⁹ Quadratic programming, one of these methods, has many disadvantages, so alternative

¹⁰ methods are studied to improve. MAD Method, an improved new method, is converted

¹¹ portfolio optimization problem into a linear programming problem. MAD Method is

- $_{12}$ $\,$ demonstrated and a case study is done by using stock certificate which belongs to BIST $\,$
- ¹³ Mining Sector.

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15 Index terms—BIST mining sector, linear programming, portfolio optimization.

16 **1** Introduction

any models have been developed in the financial literature under the heading of portfolio optimization and these
models were named as traditional portfolio and modern portfolio optimization. While attempting to minimize the
risk of the portfolio through diversification of securities too much, not minding interrelationship between them, in

20 traditional portfolio management approach; portfolio optimization has been made through mean-variance model

21 ??Markowitz, 1952:77-91) in modern portfolio management approach.

Harry Markowitz is called as the founder of the theory of modern investment with his study, by the name of "Portfolio Selection", that he presented as phd dissertation in the year 1952. In this study, Markowitz targeted the selection of the lowest-risk portfolio corresponding to a certain return on the basis of mean variances.

Various scientists attempted to develop portfolio selection model on the basis of mean -variance model. Tobin ??1958), ??harpe (1964) ve Lintner (1965) adapted real-life constraints to the model, such as investor's decision on percentage of portfolio consisting of risky assets, borrowing-lending situation, short-term sales, transaction costs and taxes. ??rennan (1971) investigated the subject of borrowing and lending; Turnbull (1977) investigated the subjects of personal taxation, uncertain inflation, nonmarket assets. ??evy (1983) and Schnabel (1984) dealt with short-term sales problem.

The difficulties caused by the increase in the number of securities for expected return of optimum portfolio and determination of variance were overcome by single index model developed by ??harpe (1963) and multiple index models developed by ??erold (1984).The studies conducted on mean-variance model revealed the Capital Assets Pricing Model (CAPM), which is both mathematical and logical extension of the meanvariance model ??Harrington, 1983). ??harpe (1964), ??intner (1965) and Mossin (1966) added moving riskfree financial asset to the model on the basis of Markowitz's studies. Konno and Yamazaki (1991) proposed the mean absolute deviation (MAD) model, which is also a portfolio optimization model, alternatively to the meanvariance portfolio

38 optimization model of Markowitz. MAD Model has used mean absolute deviation instead of variance intended to

be minimized in the objective function of mean-variance model. Thus, portfolio selection problem was degraded
from a quadratic program to a linear program (Simaan, 1997 ??Simaan, : 1437)).

In this study, it is intended to inform about MAD model proposed by Konno and Yamazaki (1991) for also solution of large-scale portfolio optimization problems that can't be solved with Markowitz's classical mean variance model and investigate its some properties. In the practice section, portfolio optimization was performed

44 through MAD model for trading securities at BIST.

45 **2** II.

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⁴⁶ 3 Mean Absolute Deviation (mad) Model

47 MAD model is an alternative method simplifying Markowitz's classical formulation by using absolute deviation 48 as a risk scale. When these two mathematically equivalent formulas have been considered in terms of calculation, 49 significant differences are noticed between them. As well as approach of risk measurement through variance 50 converts the problem to quadratic programming problem, absolute deviation approach degrades the problem to

⁵¹ linear programming problem **??**Konno ve Koshizuka, 2005: 893).

Konno and Yamazaki revealed that mean absolute deviation of normal distribution was proportional with standard deviation of that. Consequently, MAD model and Markowitz model show the same activity under the multi variability of return of assets. Provided that these returns of (R_1,R_2,?,R_n) suggest multi variability normal distribution, then these two measures are the same. In other words, when returns of (R_1, R_2,?,R_n) suggest multi variability normal distribution, it means that minimizing the function ??(??) is minimizing the function ? (x) at the same time (Simaan, 1997 **??**Simaan, : 1437)). Furthermore, Rudolf, Wolter and

⁵⁸ Zimmermann (1999) revealed that minimizing mean deviation was equivalent to maximizing expected utility in

case of avoiding risk (Rudolf et al. 1999: 85 103).

₆₀ 4 a) Mathematical Model

61 ?? ?? , (?? = 1,2, ? ??), ??. represents the random variable implying return of asset and ?? ?? , (?? = 1,2, ? 62 , ??) ??. representing the ratio to be invested to asset, total return of portfolio consisting of assets is calculated 63 as follows:??(??) = ? ?? ?? ?? ?? ?? ?? ?? =1

Here, ??. represents return of asset, ?? ?? ; asset's price at the end of the period, ?? ???1 ; asset's price at the beginning of the period?? ?? = (?? ?? ??? ???1) ?? ???1

66 , is calculated with this formula.

57 Standard deviation used as the scale of variance and risk in standard portfolio analysis is calculated as 68 follows:??(??) = ??[(??(??) ? ??[??(??)]) 2] ??(??) = ???(??)

71 5 ??

?: mimimum return desired by investor ?? ???? : ?? is the acquired return for time period ?? = (1,2,?)

90 6 Aplication

In this section, portfolio optimization was carried out through that MAD model was applied to the actual data 91 92 obtained from BIST. In the application part of this study, returns of mining sector concerned shares included in 93 the SIST index between the dates 04.01.2010 to 4.12.2014 were calculated on the basis of daily closing prices and 94 MAD model was applied to these data. It was assumed in the model that investors would create their portfolios 95 with fully risky investments and risk-free investment and short selling wouldn't be allowed. MAD model was applied to the data by being written in an econometric package program. The shares used in the study belong 96 to ?hlas Mining (IHMIN), Ipek Natural Energy (IPEKE), Koza Mining (KOZAA), Koza Gold (KOZGO), Park 97 Electric and Mining (PRKM). The statistics concerning these 5 shares have been given in Table 1. For an investor 98 targeting different returns and will make an investment on the basis of MAD model; in which ratio from which 99 shares he should invest to his portfolio have been shown in Table ??. 100

Table 2 : Minimum Risk Ratio of Shares by a different Target Return

¹⁰³ 8 Table 2 (Con't) : Minimum Risk Ratio of Shares by a different ¹⁰⁴ Target Return

The expected return and variances of these portfolios acquired for different returns using MAD model have been 105 shown in Table 3. When examined the tables, it has been seen that the shares that will make contribution 106 to portfolio in terms of profit that will be created for investor's desire and natural expectation are IHMIN, 107 KOZGO and PRKM yielding positive return. Accordingly, it is obvious that other two shares will not make 108 any contribution for profit growth. Two mainly recommended shares in the portfolios created by MAD model 109 are KOZGO and PRKM. The reason why IHMIN securities haven't been included in the optimum portfolios is 110 that there is so much risk due to excessive fluctuations between beginning of period and end of period related 111 market closing prices of the years selected. Remembering that through MAD model it is intended to minimize 112 113 the equation that is objective function, yielding mean absolute deviation; naturally, the shares to be selected are supposed to minimize the risk as well as increase profit. Therefore, not only the shares with positive returns 114 but also the ones with minimum risk were selected in optimum portfolios created by MAD model. When these 115 116 considerations taken into account, it has been noticed that MAD model has yielded positive results and can be 117 used in daily life.

On the other hand, comparing the variation coefficients (coefficient of change), another criterion in the selection of shares; it can be decided that which shares should be included in the portfolio that will be created and which ones shouldn't. Variation coefficient is defined as follows.

123 124 deviation and value of returns of the shares belonging to mine sector in question and the results of variation 125 coefficient calculated on the basis of these values. It was found in the evaluations mentioned above that IPEKE 126 and KOZGO securities' returns were negative, accordingly they shouldn't be included in the portfolios created. 127 On the basis of that, when other three shares compared, the risks of the ones that must be included in portfolio. 128 are supposed to be small as much as possible. When their variance coefficients were compared, the order from 129 high to low value would be respectively IHMIN, KOZAA, and PRKM. On the basis of that securities with small 130 variation coefficient should be included in the optimum portfolio for portfolio optimization, since IHMIN return's 131 variation coefficient is so high, KOZAA and PRKM securities are supposed to be included in the optimum 132 portfolio to be created as much as possible. When all of these taken into account, it is seen that portfolio 133 134 optimization carried out with MAD model comply with daily life and not conflict with other portfolio selection 135 criteria or methods in finance sector.

136 **10 IV**.

137 11 Conclusion

Mean-Variance Model creating major changes in Markowitz's portfolio selection understanding is a currently used quadratic programming model revealing interrelationships between assets through risk-return variation, accordingly, taking into account diversification and the evaluation of entire portfolio. MAD model proposed by Konno and Yamazaki is one of the models proposed in time to overcome several problems encountered in the selection of portfolio. In MAD model, which is a linear programming model, risk is expressed with mean absolute deviation, not with variance.

In this study, MAD model was theoretically introduced. In the study performed with actual data, daily values of returns of the securities between January 2010-December 2014 of mine sector being included in SIST's index were used and portfolios were acquired on the basis of different target returns through application of the model. Model was tested firstly comparing the fluctuations between values of returns of actual data and market closing prices; secondly, variation coefficient comparison method, which is another criterion used for selection of share in portfolio optimization, was used. It was seen according to both these two considerations that there wasn't any conflict with the consequences of the portfolios created through MAD model.

MAD model brought a new perspective to the classic portfolio optimization problem and degraded the problem to linear programming problem by defining the risk on the basis of mean absolute deviation. Thus, model has brought along the advantages such as transaction easiness, not requiring distribution assumption, ability to be reformulated for various constraints. The only disadvantage of MAD model encountered in the literature is that it can lead to prediction error due to not taking covariance matrix into account. When theoretical benefits and

Shares	Mean	Std.	Skw.	Kur.
		Dev.		
IHMAD	0,038	$0,\!050$	1,325	-5,341
IPEKE	-0,045	0,031	$1,\!291$	0,274
KOZAA	0,049	0,090	$5,\!594$	-2,584
KOZAL	0,089	0,046	3,863	1,209
PRKM	0,058	0,025	1,580	$1,\!158$

Figure 1: Table 1 :

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1

of MAD Model; in order to test the reliability of this model, Tablo4 and Tablo5 will be examined. Having constituted optimum portfolios with different minimum returns acquired through application

Figure 2: Table 3 :

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Figure 3: Table 4 :

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	Min.	Max.	Difference
IHMAD	0.64	9.8	9.16
IPEKE	1.45	6.18	4.73
KOZAA	1.48	2.32	0.84
KOZAL	12.15	48	35.85
PRKM	2.34	7.28	4.94

Figure 4: Table 5 :

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	Std. Dev.	Return	Variation Coeff.
IHMAD	$0,\!050$	0,00388	129
IPEKE	0,031	-4,5E-05	-704,72
KOZAA	0,090	0,0049	18,31
KOZAL	0,046	0,00089	$52,\!22$
PRKM	0,025	0,0058	43,725

Figure 5: Table 6 :

application performance of the model have been considered together, it has showed itself as a preferable portfolio optimization model. 1^{2} 3^{3} 156 optimization model. 157

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